

B.Sc 2nd Semester 2021

1. Answer the following

5X3=15

- a. Define alternating series. Test the following series $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n^p}$

for convergence, absolute convergence and conditional convergence

- b. Examine the convergence for the following infinite series $\sum \frac{1.3.5 \cdots (2n-1)}{2.4.6 \cdots 2n} \frac{x^{2n}}{2n}$, x

being non- negative

- c. State Cauchy's n^{th} root test. Test the convergence of the series

$$\left(\frac{2^2}{1^2} - \frac{2}{1}\right)^{-1} + \left(\frac{3^3}{2^3} - \frac{3}{2}\right)^{-2} + \left(\frac{4^4}{3^4} - \frac{4}{3}\right)^{-3} + \cdots$$